

# Minimization of Intermodulation Distortion in GaAs MESFET Small-Signal Amplifiers

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**Abstract**—This paper examines the dependence of third-order intermodulation distortion on the source-reflection coefficient,  $\Gamma_s$ , as a function of frequency in an amplifier designed according to available-gain criteria. By means of a numerical formulation of the Volterra series, a complete equivalent circuit of the FET can be used, and intermodulation calculations include all feedback effects. We show that the sensitivity of  $IP_3$  to  $\Gamma_s$  decreases with increasing frequency and can be related to the MESFET's stability.

## I. INTRODUCTION

MICROWAVE GaAs MESFET devices are used as amplifiers in a variety of linear applications. However, nonlinear properties of the MESFET's can cause two or more signals applied to the device simultaneously to produce intermodulation (IM) distortion. This distortion has important effects on system performance, particularly in broad-band communication systems. Thus, minimization of IM distortion is often a critical requirement.

In this paper we show how the IM performance of a small-signal amplifier can be optimized when the amplifier is designed according to available-gain criteria. In this process the MESFET's output is conjugate-matched and its input is mismatched to obtain a specified value of gain. We choose this method because it generally results in better dynamic range than do other options; these options are (1) matching the input and mismatching the output or (2) simultaneously matching both the input and output (which, in many cases, is impossible). In available-gain design the value of source impedance that provides the desired gain is not unique and can be selected to optimize IM levels.

In many cases the IM intercept point [1] is a valid figure of merit for IM performance. To obtain the intercept point one must first be able to predict third-order intermodulation products, which result from the nonlinearities in the circuit. Other researchers have attempted to model nonlinearities in GaAs FET's by using the harmonic-balance technique [2]–[4] or specialized, approximate techniques [5]. The Volterra series has also been used to analyze nonlinear distortion in MESFET's [6]–[9]; however, much

of this work employs simplifying approximations that reduce accuracy. For example, in the work by Gupta *et al.* [6] the second-degree terms in the Volterra-series expansions were set to zero. However, these second-order products have an effect on the third-order products and therefore must be taken into account. Minasian [7] and Lambrianou *et al.* [8] employ simplified, unilateral equivalent circuits of the MESFET.

These simplifying assumptions are employed to ease the painfully difficult task of generating Volterra kernels in algebraic form. In this work, however, we circumvent such limitations by calculating the kernels numerically; thus, no such simplifying assumptions are necessary, and we can use a complete equivalent circuit of the MESFET. Furthermore, we include the effects of all of the MESFET's feedback elements; these effects have not been examined previously. Because Volterra-series analysis operates entirely in the frequency domain, is noniterative, and requires no convergence process, it is highly efficient and thus is a practical technique for circuit optimization [10].

## II. MODELING THE MESFET

This work is based on the packaged Avantek AT10650-5 MESFET, a  $0.5 \times 250 \mu\text{m}^2$  device that is similar in structure and performance to many commercial *Ku*-band MESFET's. The MESFET chip and its package are modeled by a lumped-element equivalent circuit in which three elements—the gate-to-source capacitance, drain-to-source resistance, and controlled current source—are nonlinear. The modeling process is performed in two steps: first, the equivalent circuit's linear elements are determined and the characteristics of the nonlinear elements are measured. The dependence of the nonlinear elements on voltage is expressed via Taylor-series expansions of their current/voltage ( $I/V$ ) or charge/voltage ( $Q/V$ ) characteristics in the vicinity of their bias points.

The FET's used in this work were taken from a common fabrication lot. *S*-parameter data were measured from 45 MHz to 17 GHz, and several FET's having nearly identical *S* parameters and  $I/V$  characteristics were selected. The high-frequency data covering the range from 2 to 17 GHz were obtained with the transistor biased at a drain voltage of 3.0 V and drain current of 20 mA. The low-frequency *S* parameters were used primarily to model the drain-to-

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elements, each controlled by a single voltage; thus

$$i_d(v_g, v_d) = i_{d,g}(v_g) + i_{d,d}(v_d) \quad (4)$$

where

$$i_{d,g}(v_g) = a_1 v_g + a_2 v_g^2 + a_3 v_g^3 \quad (5)$$

and

$$i_{d,d}(v_d) = b_1 v_d + b_2 v_d^2 + b_3 v_d^3. \quad (6)$$

The  $a_n$  and  $b_n$  coefficients are the  $\partial^n I_d / \partial V_g^n$  and  $\partial^n I_d / \partial V_d^n$  terms in (1); from (1)–(3),  $a_1 \equiv g_m$  and  $b_1 \equiv G_{ds}$ . This approach is an approximation because it neglects the cross terms  $\partial^k I_d / \partial V_g^n \partial V_d^n$  in (1). Although it is clear that the cross terms are usually much smaller than the terms involving  $V_g$ , they are sometimes not small compared to those involving  $V_d$ . The terms involving  $V_d$  are rarely dominant, but may still be significant; thus, these cross terms may also be significant.

The modeling of  $i_{d,g}$  is further complicated by its weak nonlinearity, especially near the bias points that would normally be used for high-dynamic-range amplifiers. Because this nonlinearity is so weak, even small measurement uncertainty and low levels of quantization noise may obscure the curvature in  $i_{d,g}$ . Even when the noise level is low, the direct differentiation of  $i_{d,g}$  to obtain the derivatives in (1) increases the noise level and makes unreliable the derivatives beyond the second. Furthermore, least-square fitting to a polynomial, a commonly used alternative, often fails because the ill-conditioned nature of the normal equation makes the process overly sensitive to small changes in the measured  $I/V$  data.

Another problem is the well-known frequency dependence of  $G_{ds}$ , which is often attributed to traps in the MESFET's channel. These cause the value of  $G_{ds}$  measured above 1 MHz to be one fifth to one half the dc value, and to have effects on the higher derivatives  $\partial^n I_d / \partial V_d^n$  which are difficult to characterize.

Because of these effects, it is usually not possible to obtain the derivatives in (1) by dc measurements. The cross terms are even more difficult to measure than the others, so there is little choice but to neglect them and to model  $i_d(v_g, v_d)$  as two separate, singly controlled nonlinear elements. The consequences of this approach are acceptable in circuits in which  $i_{d,g}(v_g)$  is the dominant nonlinearity; this is the case in virtually all modern MESFET's.

These considerations are not unique to Volterra-series analysis. They apply to any form of analysis used to calculate small-signal nonlinear effects in FET amplifiers; in particular, to harmonic-balance analysis. Because harmonic-balance analysis is applied primarily to large-signal circuits, the models usually are designed to describe the MESFET over the entire range of drain-to-source and gate-to-source voltages. However, these models may not accurately express the derivatives in (1) in the vicinity of a specific bias point, and their use may result in incorrect results when applied to small-signal distortion problems.

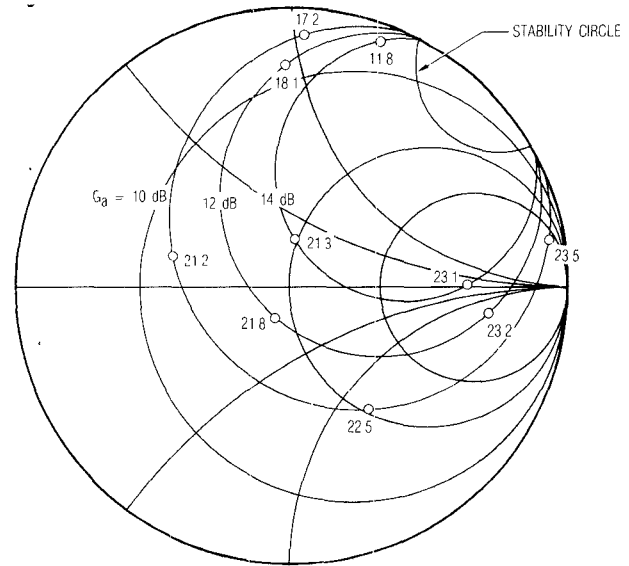


Fig. 4. Gain and stability circles and calculated third-order intercept points of the MESFET at 2 GHz.

The  $a_n$  terms in (5), which represent a nonlinear controlled current source, were determined by the method described in [13]. This method involves extracting the source's Taylor-series coefficients from harmonic measurements at low frequencies. The  $b_n$  terms in (6) represent a nonlinear conductance. These were found by numerically differentiating values of  $G_{ds}$  obtained from low-frequency  $Y$  parameters over a range of values of  $v_d$ ; because the curvature of  $G_{ds}(V_d)$  was much greater than the uncertainties in the data, and only two derivatives need be taken, a multipoint derivative formula gave good results. Because it is based partly on dc measurements, this process only partially compensates for the frequency sensitivity of  $G_{ds}$ .

The value of gate capacitance  $C_{gs}$  varies with  $V_g$ , the voltage across the capacitor's terminals.  $C_{gs}$  behaves as a uniformly doped Schottky-barrier diode capacitance having the controlling voltage  $v_g$ , and was modeled as such. The nonlinear MESFET model was established by including the nonlinearity of  $C_{gs}$ ,  $G_{ds}$ , and  $g_m$  in the linear equivalent circuit of Fig. 1. The nonlinear equivalent circuit is shown in Fig. 3.

### III. CALCULATIONS

The available gain of a two-port is a function solely of the source reflection coefficient  $\Gamma_s$ ; the locus of  $\Gamma_s$  values that provide a specific value of gain lie on a circle in the  $\Gamma_s$  plane. The available-gain and stability circles of the GaAs FET were plotted on a Smith chart for three frequencies: 2, 5, and 10 GHz. Intermodulation (IM) products were calculated at points chosen periodically along the gain circles to find values that would maximize the amplifier's third-order intercept point,  $IP_3$ . The stability circles and the corresponding intercept points are shown in Figs. 4, 5, and 6.

In order to calculate the  $IP_3$  values, it was necessary to modify the FET model to account for differences between



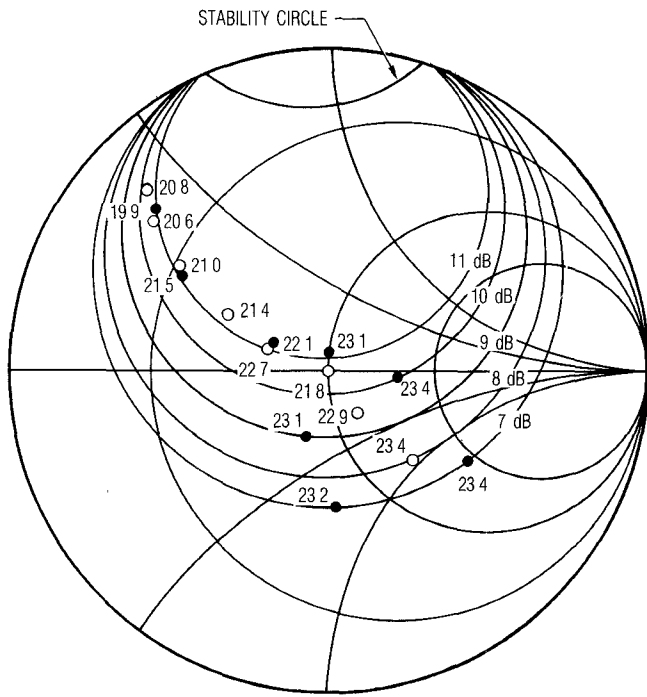


Fig. 7. Gain and stability circles and third-order intercept points of the MESFET at 5 GHz. Measured  $IP_3$  values are indicated by circles, calculated values by solid dots.

put circuit consisted of a quarter-wave transformer and a length of 50  $\Omega$  line.  $\Gamma_s$  was varied by trimming the width of the microstrip transformer; thus its impedance increased each time it was cut. The output was conjugate matched in each case by means of a tuner, and intercept points were measured via a two-tone test. In this way, the intercept points for eight  $\Gamma_s$  values were obtained.

The transformer's step-discontinuity reactances are an important component of  $\Gamma_s$ . Unfortunately, attempts to model these reactances via closed-form quasi-static approximations were not successful because of the limited accuracy of such formulations. To determine these values, we note that the dominant effect of the transformer is to change the magnitude of  $\Gamma_s$ , while the discontinuities primarily affect the phase. Thus, one can find  $|\Gamma_s|$  from the transformer impedance, and  $\angle \Gamma_s$  as the point where the  $|\Gamma_s|$  curve intersects the gain circle. This heuristic approach treats the FET's measured  $S$  parameters as a standard. This is reasonable, because the FET's  $S$  parameters—measured by an accurately calibrated automatic network analyzer—are known more accurately than the discontinuity reactances.

The experimental intercept points and the calculated data are plotted on a Smith chart in Fig. 7; the gain and  $IP_3$  values are corrected for the loss in the output tuner (0.7 dB). The difference between the calculated and measured  $IP_3$  values in most cases is less than 1 dB.

At 10 GHz, the MESFET is unconditionally stable. It is evident from Fig. 6 that the intercept points in this case do not vary much along the gain circles, or even from one gain circle to another; the distortion levels are already minimal for unconditionally stable conditions. This insen-

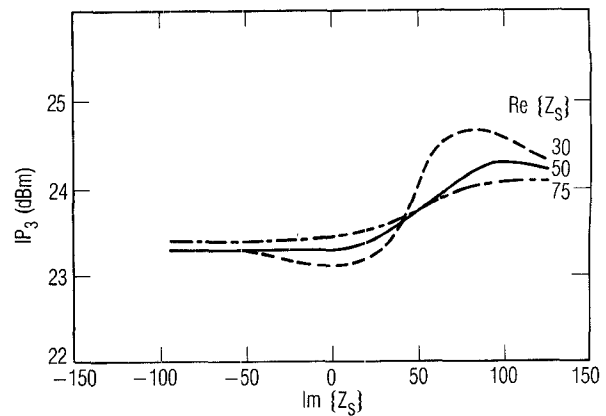


Fig. 8. Sensitivity of  $IP_3$  to  $Z_s$  at 5 GHz;  $Z_L = 65 + j86$  (this is the optimum value of  $Z_L$  when  $Z_s = 50 + j0$ ).

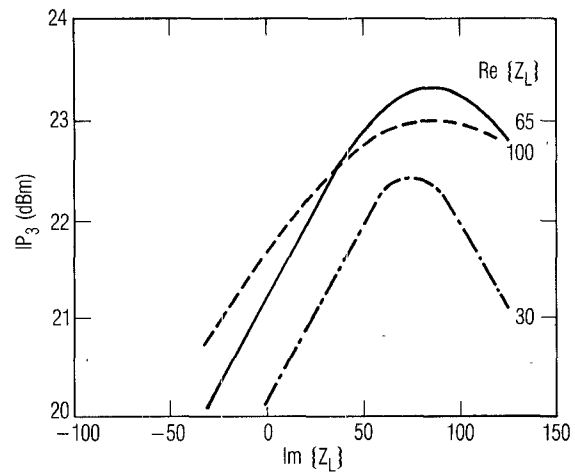


Fig. 9. Sensitivity of  $IP_3$  to  $Z_L$  at 5 GHz;  $Z_s = 50 + j0$ .

sitivity of  $IP_3$  to  $\Gamma_s$  is a characteristic of unilateral circuits [1]. We believe that the reason for the insensitivity of  $IP_3$  to  $\Gamma_s$  is a manifestation of the fact that feedback effects are minimal in an unconditionally stable circuit. Thus, in terms of its  $IP_3$  characteristics, the amplifier behaves much like a unilateral circuit.

At 5 GHz the MESFET is conditionally stable and has optimum values of  $\Gamma_s$  for minimizing third-order intermodulation distortion. Fig. 5 shows that the intercept points are highest near the counterclockwise extreme of the gain circles, and are nearly independent of gain. At the clockwise extreme, the intercepts are lower and are much more sensitive to gain; the  $IP_3$  values increase as gain decreases. In general, the intercept points are lower in regions near the stability circle.

The same conclusions can be deduced from the 2 GHz case shown in Fig. 4, except that the effects are more pronounced. The best performance is obtained near the counterclockwise end of the gain circle, and the worst performance—a 12 dB reduction in  $IP_3$ —occurs near the clockwise end.

Figs. 8 and 9 show the sensitivity of  $IP_3$  to source and load impedance when no gain constraint is imposed. It is

clear from these figures that the intrinsic sensitivity of  $IP_3$  to load impedance is much greater than the sensitivity to source impedance. (However, if  $IP_3$  were defined in terms of available input power instead of output power, a definition that sometimes is more relevant, the sensitivity to  $\Gamma_s$  would be greater.) This sensitivity to load impedance is reflected in the data of the earlier figures: at 10 GHz, where the FET is unconditionally stable and thus feedback effects are minimal, the value of  $\Gamma_L$  that results in a conjugate match is close to  $S_{2,2}^*$  and does not vary much as  $\Gamma_s$  is varied. Consequently, the  $IP_3$  does not vary significantly with  $\Gamma_s$ . However, at 5 GHz the FET is conditionally stable and  $\Gamma_L$  varies more strongly with  $\Gamma_s$ ; the sensitivity of  $\Gamma_L$  to  $\Gamma_s$  is especially severe at 2 GHz. It is interesting to note that the worst values of  $IP_3$  are strongly associated with highly reactive values of  $\Gamma_L$ . These results are consistent with an experimental study of IM in MESFET's that identified  $\Gamma_L \approx S_{2,2}^*$  as a good estimate of the load impedance that maximized  $IP_3$  [14].

Fortunately, the values of  $\Gamma_s$  that optimize intercept point are generally in the same region of the input plane as those that optimize noise figure. Thus, at a given bias level the trade-off between noise and linearity in a FET amplifier may not be very severe. However, the bias conditions that optimize noise figure ( $I_d \approx 0.15I_{dss}$ ) and those that optimize  $IP_3$  ( $I_d \approx 0.50I_{dss}$ ) present a substantial trade-off.

### V. CONCLUSIONS

These results show that this approach to optimizing intercept points is practical and accurate. The measured and predicted intercept points fall within approximately 1.5 dB of each other, which is little more than the uncertainty in the measurements themselves. The use of a complete MESFET model makes the results particularly meaningful, because no significant effects related to the circuit topology (e.g., feedback phenomena) are ignored.

Under available-gain constraints, the MESFET's output  $IP_3$  is sensitive to  $\Gamma_s$ . At low frequencies, where the MESFET is conditionally stable, the MESFET's  $IP_3$  is most sensitive to  $\Gamma_s$ . However, as frequency is increased, that sensitivity decreases and essentially disappears at the point where the MESFET becomes unconditionally stable. This sensitivity is the result of feedback effects that cause the conjugate-match  $\Gamma_L$  to be highly reactive. When gain constraints are removed, the sensitivity of output  $IP_3$  to  $\Gamma_L$  is greater than the sensitivity to  $\Gamma_s$ .

Conventional methods of modeling the drain-current nonlinearity do not include potentially significant effects in the device. Further research is needed to develop more accurate modeling techniques.

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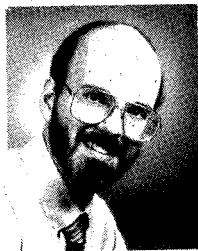
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